

30 points	25 points	25 points	25 points	105 points
1	2	3	4	<b>Total</b>

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# MATH 102 CALCULUS II

**03.06.2011**

İzmir University of Economics Faculty of Arts and Sciences, Department of Mathematics

## FINAL EXAM

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**Student Name and Department:** .....

**Section:** Check for your instructor and course program below:

- Halil ORUÇ, Friday 08:30 – 11:20
- Halil ORUÇ, Friday 12:30-15:20
- Gökhan BİLHAN, Wednesday, 8:30-11:20
- Gökhan BİLHAN, Wednesday, 12:30-15:20
- İbrahim Çanak, Thursday 8:30-11:20, Tues. 12:30-15:20
- İlgin SAĞER, Monday, 08:30–11:20, 12:30–15:20
- İlgin SAĞER, Tuesday, 15:30–18:20
- İlgin SAĞER, Wednesday, 12:30–15:20

Good Luck...

1. (10+10+10 pt) Evaluate the following integrals

(a)  $\int_0^\pi \sqrt[3]{\cos x} \sin x \, dx = ?$

(b)  $\int_0^\pi x \cos x \, dx = ?$

(c)  $\int_0^2 \int_{x^2}^4 \frac{4x}{1+y^2} \, dy \, dx = ?$

SOLUTION:

2. (25pt) A manufacturing company in Manisa produces two models of an HDTV per week,  $x$  units of model  $A$  and  $y$  units of model  $B$  at a cost (in TL) of

$$C(x, y) = 6x^2 + 12y^2$$

if it is necessary (because of shipping considerations) that

$$x + y = 90$$

how many of each type of set should be manufactured per week to minimize cost?  
What is the minimum cost?

SOLUTION:

3. (25pt) First sketch graphs of the region then Find the volume of the solid under the graph of  $f(x, y) = 4xy$  over the region bounded by the graphs of  $R = \{(x, y) : y = \sqrt{1 - x^2}, y = 0, 0 \leq x \leq 1\}$

SOLUTION:

4. (25pt) A rectangular box with no top and two intersecting partitions (see the figure) must hold a volume of 72 cubic inches. Find the dimensions that will require the least amount of material?

SOLUTION: